Formula	Sheet	for	Math	151,	Exam	<b>2</b>
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Lines: If $(x_1, y_1), (x_2, y_2)$ lie on a line L, the slope of L is $m = \frac{y_2 - y_1}{x_2 - x_1}$ and the equation is $y - y_1 = m(x - x_1)$ .
Distance: $(x_1, y_1)$ to $(x_2, y_2)$ : $\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$ . Circle, center $(a, b)$ , rad. $r$ : $(x - a)^2 + (y - b)^2 = r^2$ .
Trig: In a right triangle: $\sin \theta = \frac{opp}{hyp} \cos \theta = \frac{adj}{hyp} \tan \theta = \frac{opp}{adj} = \frac{\sin \theta}{\cos \theta} \cot \theta = \frac{1}{\tan \theta} \sec \theta = \frac{1}{\cos \theta} \csc \theta = \frac{1}{\sin \theta}.$
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Periodicity: $\sin(x + 2\pi) = \sin(x)$ , $\cos(x + 2\pi) = \cos(x)$ , $\tan(x + \pi) = \tan(x)$ . Identities: $\sin^2 x + \cos^2 x = 1$ , $1 + \tan^2 x = \sec^2 x$ , $\sin(2x) = 2 \sin x \cos x$ , $\cos(2x) = \cos^2 x - \sin^2 x$ .
Addition: $\sin(x\pm y) = \sin x \cos y \pm \cos x \sin y$ $\cos(x\pm y) = \cos x \cos y \mp \sin x \sin y$ $\pi \approx 3.1416.$
Exponentials and logarithms: $a, b, t, u, y > 0, r, v, w, x$ any real numbers: $a^{v+w} = a^v a^w, a^{vw} = (a^v)^w, a^{-v} = 1/a^v, a^0 = 1, (ab)^v = a^v b^v, \log_a(t) = \ln(t)/\ln(a).$ $e^x = y$ is equivalent to $x = \ln y, e^{\ln y} = y, \ln(e^x) = x.$ $\ln(tu) = \ln(t) + \ln(u), \ln(u^r) = r \ln(u), \ln(1/u) = -\ln(u), \ln(1) = 0, e \approx 2.718.$
Squeeze Theorem: If $f(x) \le g(x) \le h(x)$ near $x = a$ and $\lim_{x \to a} f(x) = \lim_{x \to a} h(x) = L$ , then $\lim_{x \to a} g(x) = L$ .
Intermediate Value Theorem: If $f$ is continuous on $[a, b]$ and $N$ is between $f(a)$ and $f(b)$ , there is a number $c$
in $[a, b]$ , such that $f(c) = N$ . Corollary: If f changes sign from a to b, then $f(c) = 0$ with c between a and b.
Definition of the Derivative: $f'(x) = \lim_{h \to 0} (f(x+h) - f(x))/h;  f'(a) = \lim_{x \to a} (f(x) - f(a))/(x-a).$
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Rules of Differentiation: $\frac{d}{dx}(cu) = c\frac{du}{dx}$ , $c$ a const., or $(cf)'(x) = cf'(x)$ . $\frac{d}{dx}(u+v) = \frac{du}{dx} + \frac{dv}{dx}$ , or $(f+g)'(x) = f'(x) + g'(x)$ . Product Rule: $\frac{d}{dx}(uv) = u\frac{dv}{dx} + v\frac{du}{dx}$ , or $(fg)'(x) = f(x)g'(x) + f'(x)g(x)$ .
Quotient Rule: $\frac{d}{dx}(u/v) = \left(v\frac{du}{dx} - u\frac{dv}{dx}\right)/v^2$ , or $(f/g)'(x) = (g(x)f'(x) - f(x)g'(x))/(g(x)^2)$ .
Chain Rule: If $y = f(u)$ and $u = g(x)$ , then $\frac{dy}{dx} = \frac{dy}{du}\frac{du}{dx}$ , or $(f \circ g)'(x) = f'(g(x))g'(x)$ . Replacing x by
<i>u</i> and multiplying by $\frac{du}{dx}$ , we can apply the Chain Rule to all boxed derivative formulas. Some examples are: $\frac{d}{dx}(u^r) = ru^{r-1}\frac{du}{dx}, \frac{d}{dx}(e^u) = e^u\frac{du}{dx}, \frac{d}{dx}(\ln u) = \frac{1}{u}\frac{du}{dx}, \frac{d}{dx}(\sin u) = (\cos u)\frac{du}{dx}, \frac{d}{dx}(\cos u) = -(\sin u)\frac{du}{dx}, \frac{d}{dx}(\tan u) = (\sec^2 u)\frac{du}{dx}.$
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