

## **Topic I: Comparison and Metric Riemannian Geometry**

### **1. Sectional curvature comparison (local version)**

Metric and Hessian comparison

Jacobi fields comparison and injective radius estimate

Topology of manifolds with negative/nonpositive sectional curvature

Synge's trick on positive sectional curvature

### **2. Ricci curvature comparison**

Laplacian comparison

Relative volume comparison and applications

Splitting theorem

### **3. Sectional curvature comparison (global version)**

Toponogov theorem

Gromov's short basis and bounding number for generators of  $\pi_1$

Critical point theory and applications

Soul theorem

### **4. Gromov-Hausdorff topology**

Gromov-Hausdorff distance and approximations

Precompactness theorem

Equivariant Gromov-Hausdorff distance

Pointed Gromov-Hausdorff distance

### **5. Convergence theory for manifolds with bounded sectional curvature**

Fibration theorem

Harmonic radius estimate and  $C^{1,\alpha}$ -convergence theorem

Singular fibration theorem

## **Topic II: Symplectic Geometry**

### **1. Symplectic manifolds**

Symplectic manifolds and Lagrangian submanifolds

Darboux-Moser theorems

Hamiltonian vector fields and Poisson brackets

### **2. Complex structures**

Compatible almost complex structures

Complex manifolds and Kahler manifolds

Dolbeault cohomology

### **3. Moment maps**

Hamiltonian group actions

Symplectic reduction

Existence and uniqueness of moment maps