

# Oral Qualifying Examination Syllabus

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## Algebraic Number Theory

1. Invariants of number fields: embeddings, discriminants and orders
2. Arithmetic of orders in number fields: fractional ideals, splittings of primes, ramification
3. Ideal Class Group of number fields
4. Structure of units in orders of number fields

## Elliptic Curves

1. The group law for adding points on an elliptic curve
2. The group of rational solutions to  $E : y^2 = x^3 + Ax + B$  form a finitely generated group (the Mordell-Weil group of  $E$ )
3. Effective bounds on the rank of the Mordell-Weil group
4. Conjectural effective algorithms to find all rational solutions to  $y^2 = x^3 + Ax + B$
5.  $L$ -series of elliptic curves and relations to modular curves
6. Applications to classical Diophantine problems

## Modular Forms

1. Elliptic Modular Curves as Riemann Surfaces
2. Elliptic Functions
3. Modular Functions and Modular Forms
4. Hecke Operators

# Automorphic Forms

1. Discontinuous groups
2. Automorphic Forms
3. Eisenstein series
4. Spectral theorem
5. Trace formula
6. Estimates for the Fourier coefficients of cusp forms
7. Automorphic  $L$ -functions