Introduction

The prerequisites needed for reading this material are "just" some high-school algebra and knowledge of simple analytic geometry. And intelligence and concentration. I will try to present interesting material which is useful and new. Some sources of what's here are hundreds of years old, but all the topics investigated are objects of current research, and are basic to current applications. These topics are usually addressed in advanced undergraduate or graduate courses. Although the methods are elementary, the results are amazing and sometimes nearly unbelievable. There are many possibilities for students to contribute to these areas – but be aware that many smart and hardworking people are working on this material. Some college courses discussing the ideas that follow are entitled

Cryptography
Probability
Networks
Combinatorics
Coding Theory
Algorithms

but I won't feel strictly bound by names of subjects: I'll try to tell you about interesting ideas and how these ideas are used. I'll touch on some of the social questions involved. I won't give complete discussions about any of these subjects. I'll try to present some good stuff. I will give further references, both to traditional sources such as books and to "new media" such as web links. Please report corrections to these notes and please suggest improvements. I will happily acknowledge all such communications.

Although I wrote that prerequisites for understanding this material are minimal, a quote on "high school" algebra from Carl Jung's *Memories, Dreams, Reflections** may be interesting.

> *... All my life it remained a puzzle to me why it was that I never managed to get my bearings in mathematics when there was no doubt whatever that I could calculate properly. Least of all did I understand my own* moral *doubts concerning mathematics.*
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> *Equations I could comprehend only by inserting specific numerical values in place of the letters and verifying the meaning of the operation by actual calculation. As we went on in mathematics I was able to get along, more or less, by copying out algebraic formulas whose meaning I did not understand, and by memorizing where a particular combination of letters had stood on the blackboard. I could no longer make headway by substituting numbers, for from time to time the teacher would say, "Here we put the expression so-and-so," and then he would scribble a few letters on the blackboard. I had no idea where he got them and why he did it–the only reason I could see was that it enabled him to bring the procedure to what he felt was a satisfactory conclusion. I was so intimidated by my incomprehension that I did not dare to ask any questions.*
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> *Mathematics classes became sheer terror and torture to me. ...*

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* Carl Jung (1875-1961) was a founder of modern psychiatry. For more information see `http://www.ship.edu/~cgboeree/jung.html`.