

Lines: If  $(x_1, y_1), (x_2, y_2)$  lie on a line  $L$ , the slope of  $L$  is  $m = \frac{y_2 - y_1}{x_2 - x_1}$  and the equation is  $y - y_1 = m(x - x_1)$ .

Distance from  $(x_1, y_1)$  to  $(x_2, y_2)$ :  $\sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$ .

Circle, center  $(a, b)$ , radius  $r$ :  $(x - a)^2 + (y - b)^2 = r^2$ .

Trig: In a right triangle:  $\sin \theta = \frac{opp}{hyp}$   $\cos \theta = \frac{adj}{hyp}$   $\tan \theta = \frac{opp}{adj} = \frac{\sin \theta}{\cos \theta}$   $\cot \theta = \frac{1}{\tan \theta}$   $\sec \theta = \frac{1}{\cos \theta}$   $\csc \theta = \frac{1}{\sin \theta}$ .

$x$	0	$\pi/6$	$\pi/4$	$\pi/3$	$\pi/2$	$\pi$	$3\pi/2$	$2\pi$	$x$	0	$\pi/6$	$\pi/4$	$\pi/3$	$\pi/2$	$\pi$	$3\pi/2$	$2\pi$	$\sin(x + 2\pi) = \sin(x)$
$\sin x$	0	1/2	$1/\sqrt{2}$	$\sqrt{3}/2$	1	0	-1	0	$\cos x$	1	$\sqrt{3}/2$	$1/\sqrt{2}$	1/2	0	-1	0	1	$\cos(x + 2\pi) = \cos(x)$

Identities:  $\sin^2 x + \cos^2 x = 1$ ,  $1 + \tan^2 x = \sec^2 x$ .

Double Angle:  $\sin(2x) = 2 \sin x \cos x$ ,  $\cos(2x) = \cos^2 x - \sin^2 x$ .

Addition:  $\sin(x \pm y) = \sin x \cos y \pm \cos x \sin y$   $\cos(x \pm y) = \cos x \cos y \mp \sin x \sin y$   $\pi \approx 3.1416$ .

Exponentials and logarithms:  $a, b, t, u, y > 0$ ,  $r, v, w, x$  any real numbers:  $a^{v+w} = a^v a^w$ ,  $a^{vw} = (a^v)^w$ ,  $a^{-v} = 1/a^v$ ,  $a^0 = 1$ ,  $(ab)^v = a^v b^v$ ,  $\log_a(t) = \ln(t)/\ln(a)$ .  $e^x = y$  is equivalent to  $x = \ln y$ ,  $e^{\ln y} = y$ ,  $\ln(e^x) = x$ .  $\ln(tu) = \ln(t) + \ln(u)$ ,  $\ln(u^r) = r \ln(u)$ ,  $\ln(1/u) = -\ln(u)$ ,  $\ln(1) = 0$ ,  $e \approx 2.718$ .

Squeeze Theorem: If  $f(x) \leq g(x) \leq h(x)$  near  $x = a$  and  $\lim_{x \rightarrow a} f(x) = \lim_{x \rightarrow a} h(x) = L$ , then  $\lim_{x \rightarrow a} g(x) = L$ .

Intermediate Value Theorem: If  $f$  is continuous on  $[a, b]$  and  $N$  is any number between  $f(a)$  and  $f(b)$ , there is a number  $c$  in  $[a, b]$ , such that  $f(c) = N$ .

Corollary: If  $f$  changes sign from  $a$  to  $b$ , then  $f(c) = 0$  with  $c$  between  $a$  and  $b$ .

Definition of the Derivative:  $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$ ;  $f'(a) = \lim_{x \rightarrow a} \frac{f(x) - f(a)}{x - a}$ .

$f(x)$	$f'(x)$	$f(x)$	$f'(x)$	$f(x)$	$f'(x)$	$f(x)$	$f'(x)$
$c$ , const.	0	$a^x$	$(\ln a)a^x$	$\tan x$	$\sec^2 x$	$\sin^{-1}(x)$	$1/\sqrt{1-x^2}$
$x^r$	$rx^{r-1}$	$\log_a(x)$	$1/(\ln(a) \cdot x)$	$\sec x$	$\sec x \tan x$	$\tan^{-1}(x)$	$1/(x^2 + 1)$
$e^x$	$e^x$	$\sin x$	$\cos x$	$\cot x$	$-\csc^2 x$	$\sec^{-1}(x)$	$1/(x\sqrt{x^2-1})$
$\ln x$	$1/x$	$\cos x$	$-\sin x$	$\csc x$	$-\csc x \cot x$	$\cos^{-1}(x)$	$-1/\sqrt{1-x^2}$

Rules of Differentiation:  $\frac{d}{dx}(cu) = c\frac{du}{dx}$ ,  $c$  a const., or  $(cf)'(x) = cf'(x)$ .

$\frac{d}{dx}(u+v) = \frac{du}{dx} + \frac{dv}{dx}$ , or  $(f+g)'(x) = f'(x) + g'(x)$ .

Product Rule:  $\frac{d}{dx}(uv) = u\frac{dv}{dx} + v\frac{du}{dx}$ , or  $(fg)'(x) = f(x)g'(x) + f'(x)g(x)$ .

Quotient Rule:  $\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{v\frac{du}{dx} - u\frac{dv}{dx}}{v^2}$ , or  $(f/g)'(x) = (g(x)f'(x) - f(x)g'(x))/(g(x)^2)$ .

Chain Rule: If  $y = f(u)$  and  $u = g(x)$ , then  $\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$ , or  $(f \circ g)'(x) = f'(g(x))g'(x)$ . Replacing  $x$  by  $u$  and multiplying by  $\frac{du}{dx}$ , the chain rule applies to all formulas in the list above. The most common examples are:

$$\frac{d}{dx}(u^r) = ru^{r-1} \frac{du}{dx} \quad \frac{d}{dx}(e^u) = e^u \frac{du}{dx} \quad \frac{d}{dx}(\ln u) = \frac{1}{u} \frac{du}{dx}$$

$$\frac{d}{dx}(\sin u) = \cos u \frac{du}{dx} \quad \frac{d}{dx}(\cos u) = -\sin u \frac{du}{dx} \quad \frac{d}{dx}(\tan u) = \sec^2 u \frac{du}{dx}$$

Bodies in Free Fall. The distance above ground level of a body in free fall in the earth's atmosphere is  $s(t) = s_0 + v_0 t - gt^2/2$ , where  $s_0$  is the position at time  $t = 0$ ,  $v_0$  is the velocity at time  $t = 0$ , and  $g$  is the acceleration due to gravity with  $g = 32\text{ft/s}^2$  or  $g = 9.8\text{m/s}^2$ .