

1. Suppose $5x^3y - 3xy^2 + y^3 = 6$. $(1, 2)$ is a point on this curve. Is the curve concave up or concave down at $(1, 2)$?

Explicit way to go y can be solved as a function of x .^{*} Then you can differentiate the formula twice and evaluate when $x = 1$.

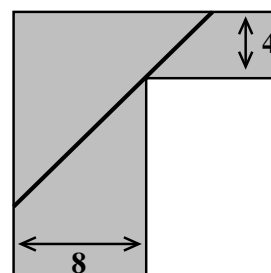
Implicit way to go Find $\frac{dy}{dx}$ implicitly and then differentiate again to get $\frac{d^2y}{dx^2}$. Evaluate everything at $(1, 2)$.

2. Questions about asymptotic growth “near” ∞ occur naturally when computer scientists analyze algorithms. One seemingly simple problem is sorting. How many comparisons are required to sort a list of n numbers? *Sorting and Searching*, volume 3 of *The Art of Computer Programming*, by D. Knuth, gives the following average running times for several sorting algorithms as a function of n :

Name	Running time
Comparison	$4n^2 + 10n$
Merge exchange	$3.7n(\ln n)^2$
Heapsort	$23.08n \ln n + 0.2n$

Which sorting method would you rather use if, in your application, $10 \leq n \leq 20$ (e.g., sorting a bridge hand)? Which would you rather use if $100 \leq n \leq 150$ (e.g., sorting grades in a lecture course)? Which would you rather use if $n \approx 10^6$ (e.g., sorting license plate numbers in New Jersey)? What happens to these functions as $n \rightarrow \infty$?

3. Find the maximum length of a pole that can be carried around a corner joining corridors of width 8 ft and 4 ft. (This is problem 59 of section 4.6 in the text.)



One problem will be selected for a writeup to be handed in at the next recitation meeting. Please see Professor Greenfield’s Math 151 webpage to learn which problem to hand in. This week only there will be a **VERY SPECIAL OFFER** which you should consider carefully.

^{*} Here it is (really!):

$$y = \left(-\frac{5}{2}x^4 + 3 + x^3 + \frac{1}{18}\sqrt{1500x^9 - 675x^8 - 4860x^4 + 2916 + 1944x^3} \right)^{1/3} - \frac{\frac{5}{3}x^3 - x^2}{\left(-\frac{5}{2}x^4 + 3 + x^3 + \frac{1}{18}\sqrt{1500x^9 - 675x^8 - 4860x^4 + 2916 + 1944x^3} \right)^{1/3}} + x$$