

Formulas for exam #1

| Function | Laplace Transform |
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| $f(t)$ | $F(s) = \int_0^\infty e^{-st} f(t) dt$ |
| $af(t) + bg(t)$ | $aF(s) + bG(s)$ |
| t^n (pos. int. n) | $\frac{n!}{s^{n+1}}$ |
| e^{at} | $\frac{1}{s - a}$ |
| $\sin(at)$ | $\frac{a}{s^2 + a^2}$ |
| $\cos(at)$ | $\frac{s}{s^2 + a^2}$ |
| $e^{at} f(t)$ | $F(s - a)$ |
| $H(t - a)f(t - a)$ | $e^{-as} F(s)$ |
| $f'(t)$ | $sF(s) - f(0^+)$ |
| $f^{(n)}(t)$ | $s^n F(s) - s^{n-1} f(0) - \dots - f^{(n-1)}(0)$ |
| $(f * g)(t) = \int_0^t f(t - \tau)g(\tau) d\tau$ | $F(s)G(s)$ |
| $\delta(t)$ | 1 |
| $\int_0^t f(w) dw$ | $\frac{1}{s} F(s)$ |
| $t^n f(t)$ | $(-1)^n \frac{d^n}{ds^n} F(s)$ |