Problem statement A rectangular box is to be constructed with volume one cubic yard. The material used in the top and bottom costs a dollars per square yard, in the front and back b dollars per square yard, and in the sides c dollars per square yard. Find the dimensions which will produce the cheapest box.