

**Problem statement** Suppose  $C$  is a *positive* real number, and  $f(x) = C - x^4$ .

a) Sketch the region **R** bounded by  $y = f(x)$  and the  $x$ - and  $y$ -axes in the first quadrant. Label the region **R**.

b) Compute the area of **R**. Your answer will use the parameter  $C$ .

c) Suppose **R** is revolved around the  $y$ -axis. Find the volume of this solid object. Your answer will use the parameter  $C$ .

d) For which value of  $C$  will the volume found in c) be equal to 1?