

Problem statement a) Suppose $f(x, y) = x^y$. Rewrite f as a composition of standard functions, and then find the domain of f and the first partial derivatives of f in its domain. Surely $2^3 = 8$. If x is increased by .01 (so (x, y) changes from $(2, 3)$ to $(2.01, 3)$), approximate the change in f using linear approximation. If y is increased by .01 (so (x, y) changes from $(2, 3)$ to $(2, 3.01)$), approximate the change in f using linear approximation. Compare the “exact answers” to the linearization answers.

b) Suppose $g(x, y, z) = x^{(y^z)}$. Rewrite g as a composition of standard functions, and then find the domain of g and the first partial derivatives of g in its domain. Surely $2^{(3^4)} \approx 2.417 \cdot 10^{24}$ (it is *exactly* 24178 51639 22925 83494 12352.). If one of the variables in g is increased by .01, which variable will likely make the biggest change in the value of g ? Support your assertion by an argument using linear approximation based on the derivatives which have been calculated. The exact values of g are not requested, but only a decision based on the linearized approximations to the perturbed function values.