

**Problem statement** a) Create a two-dimensional force field  $\mathbf{F} = M\mathbf{i} + N\mathbf{j}$  defined on all of  $\mathbf{R}^2$  *except*  $(0, 0)$  with the following properties:

- i)  $\mathbf{F}$  is *always* perpendicular to the level curves of the function  $g(x, y) = x^2 + 4y^2$ .
- ii) The magnitude of  $\mathbf{F}$  at  $(x, y)$  is inversely proportional to the distance of  $(x, y)$  to the origin.
- iii)  $\mathbf{F}$  at  $(1, 0)$  is  $\mathbf{i}$ .

b) Compute  $\int_C M dx + N dy$  where  $C$  is the curve given  $\begin{cases} x = 2 \cos(t^{78}) \\ y = \sin(t^{78}) \end{cases}$ ,  $.34 \leq t \leq .56$ .  
(Think physically!)