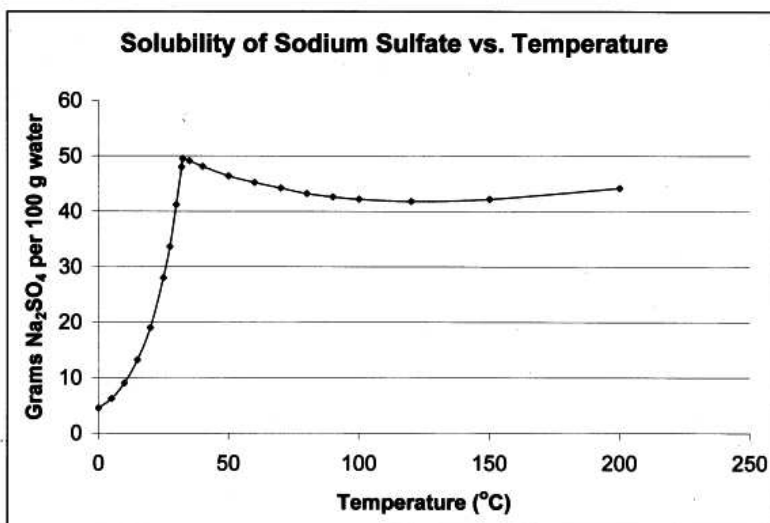


**Problem statement** The amount of a substance which can be dissolved in a solution may vary with temperature. Below is a graph of the solubility (the maximum amount of the substance) in grams of sodium sulfate,  $\text{Na}_2\text{SO}_4$ , which can be dissolved in 100 grams of water as a function of temperature in degrees Celsius. Suppose  $S(T)$  is the solubility at temperature  $T$ . Use the graph to answer the following questions as well as you can.



- Where is  $S(T)$  continuous? Where is  $S(T)$  differentiable?
- Where is  $S(T)$  increasing? Where is it decreasing? Does  $S(T)$  have any local extrema? If yes, where and what type?
- In what intervals is  $S(T)$  concave up? In what intervals is  $S(T)$  concave down? Does  $S(T)$  have any points of inflection?
- Sketch a graph of  $S'(T)$ . What are the units on each axis of your graph?