Problem statement Here are some approximate values:

$$\ln 2 \approx .7 \text{ and } \ln 10 \approx 2.3 \,.$$

Use these approximations and an indirect argument using only arithmetic to explain how many decimal digits to expect in the number 2^{40}. Are you correct?