

**Problem statement** Questions about asymptotic growth “near”  $\infty$  occur naturally when computer scientists analyze algorithms. One seemingly simple problem is sorting. How many comparisons are required to sort a list of  $n$  numbers? *Sorting and Searching*, volume 3 of *The Art of Computer Programming*, by D. Knuth, gives the following average running times for several sorting algorithms as a function of  $n$ :

<b>Name</b>	<b>Running time</b>
Comparison	$4n^2 + 10n$
Merge exchange	$3.7n(\ln n)^2$
Heapsort	$23.08n \ln n + 0.2n$

Which sorting method would you rather use if, in your application,  $10 \leq n \leq 20$  (e.g., sorting a bridge hand)? Which would you rather use if  $100 \leq n \leq 150$  (e.g., sorting grades in a lecture course)? Which would you rather use if  $n \approx 10^6$  (e.g., sorting license plate numbers in New Jersey)? What happens to these functions as  $n \rightarrow \infty$ ?