

**Problem statement** The function  $S$  (the “squaring function”) has domain all real numbers and is defined by the formula  $S(x) = x^2$  for all  $x$ .

a) Consider the function  $T$  whose domain is also all real numbers which is defined by

$$T(x) = \begin{cases} S(x) & \text{if } x \neq 3 \\ 7 & \text{if } x = 3 \end{cases}.$$

Sketch a graph of  $T$ . What is  $\lim_{x \rightarrow 5} T(x)$ ? What is  $\lim_{x \rightarrow 3} T(x)$ ? Support your assertions.

b) An evil interstellar visitor *changes exactly one million values* of  $S$  and creates a new function,  $V$ . What can be said about  $\lim_{x \rightarrow a} V(x)$  for all values of  $a$ ? Support your assertions.