

**Problem statement** Consider the function  $f(x) = e^x \sin Nx$  on the interval  $[0, 1]$  where  $N$  is a positive integer.

a) With a sketch or otherwise, describe the graph of this function when  $N = 5$ ,  $N = 10$ , and  $N = 100$ .

b) Compute  $\int_0^1 f(x) dx$ . Evaluate this integral when  $N = 5$ ,  $N = 10$ , and  $N = 100$ .

c) What happens to the graph and to the value of the integral as  $N \rightarrow \infty$ ? Does the graph confirm the limiting behavior of the integral's value?